

Original Research

Modelling the architecture of hazelnut (*Corylus avellana*) Tonda di Giffoni over two successive years

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Abstract. Hazelnut (*Corylus avellana*) cultivation is increasing worldwide. A 3D model of its structure could improve managerial techniques such as pruning. This study aims to analyse, over two successive years, hazelnut architectural development to implement a functional structural plant model. One hundred and four one-year-old shoots of own-rooted hazelnut trees were selected and analysed in winter 2020 and 2021. Exploratory analyses, generalized linear models and multinomial regression models were used to describe the architectural processes. The existence of sylleptic shoots on hazelnut one-year-old shoots, characterized by the presence of the male inflorescence on apical position, was detected. Along proleptic shoots, the branching pattern was described by (i) blind nodes located in the proximal part (ii) sylleptic shoots and mixed buds in the median part (iii) vegetative buds in the distal part. Apical bud died during the growing season, suggesting that Tonda di Giffoni has a sympodial branching. The models revealed dependencies among buds located at the same node, in the case of proleptic shoots. Especially, the probability of a bud bursting depended on both its type (i.e. mixed or vegetative) and the presence of other buds, either mixed or vegetative. Based on these local models and on a flow diagram, which defines the steps that led to the construction of hazelnut tree architecture, the first functional–structural plant model of hazelnut tree architecture was built. Further experiments will be needed and should be repeated over the following years to extend this study towards the juvenile phase and tree architecture over time.

KEYWORDS: Architecture; branching; buds; *Corylus avellana*; growth; hazelnut tree; modelling.

1. INTRODUCTION

In recent decades, functional–structural plant models (FSPMs) have been developed to describe the growth and development of trees and crops (DeJong 2019; Louarn and Song 2020). FSPMs have the peculiarity of coupling two different sub-models: one reproducing the architectural part of the tree or crop and the other simulating its functions, in interaction with environmental conditions (Room *et al.* 1996; Sievänen *et al.* 2014). The construction of an FSPM, usually, starts from the architectural part to which physiological models are added (for reviews, see Grisafi *et al.* (2021) and Vos *et al.* (2010)). Architecture has a crucial role in the growth and development of a fruit tree crop. Indeed, it influences how the light reaches the leaves in the canopy and, consequently, the photosynthetic process. It determines where

the different organs are within the plant and, therefore, the carbon partitioning. Thus, knowing the position of the flowers on the branches and, consequently the location of the fruits, enables defining where the production is and how fruits can receive water and carbohydrates during their development.

Hazelnut is an emerging fruit crop and its cultivation is increasing worldwide (FAOSTAT 2020). The world leader producer is Turkey, followed by Italy, USA and Azerbaijan (FAOSTAT 2020). In Italy, ‘Tonda di Giffoni’ is one of the most appreciated cultivars, thanks to its nut quality (Pettriccione *et al.* 2010). Despite its importance, few attempts have been made to model its development so far. A process-based model that simulates the yield was recently developed (Bregaglio *et al.* 2020), but, nowadays, a structural model is still missing. Architectural analyses

of several fruit tree crops, such as almond (Negrón et al. 2013), kiwifruit (Cieslak et al. 2007) and apple (Costes et al. 2008) have already been performed. However, few architectural studies have been achieved on bushy trees, except on the coffee tree (Motisi et al. 2019) and on the ornamental rose plant (Crespel et al. 2013). Since hazelnut (*Corylus avellana*) has a bushy shape, this study could be particularly interesting for this species.

Hazelnut is a monoecious species with male flowers, grouped into inflorescences called catkins, and female flowers, grouped into inflorescences, called glomerules, which are located in mixed buds. Male and female flowers bloom in full winter while the fecundation process occurs in late spring. During this period of time, bud breaking occurs followed by stem elongation. Along one-year-old shoots, the successive nodes can be latent, bear a sylleptic shoot with male flowers (catkin) or have more than one axillary buds whose fate can be mixed, or vegetative. Vegetative buds will give birth, the following year, to a new vegetative shoot called proleptic shoot. Mixed buds behave as vegetative buds except for the presence of the glomerules at their apex that, if the fecundation succeeds, will become a cluster of nuts (Germain and Sarraquigne 2004). Several studies describe the biology and physiology of the reproductive organs of hazelnuts (Mehlenbacher 1991; Germain 1994). However, they paid no attention to the dynamic of axillary shoot emergence and the position of catkins in sylleptic shoots that is, shoot developing immediately without a resting period (Germain and Sarraquigne 2004).

Plant structure is the result of two fundamental processes: **apical growth** from the apical meristem and **branching processes** from axillary meristems (Gifford and Foster 1987). In perennial plants growing in temperate climates, those processes are usually investigated, over different years, during winter because the plant structure is more accessible without leaves. To investigate branching, it has been proposed to focus on one-year-old shoots and record the type of bud at each node (Godin et al. 1997; Costes and Guédon 2002). The node scale is appropriate when there is a strong effect of its position along the shoot on the type of bud and the development of new shoots (Caraglio and Barthélémy 1997). Moreover, the position of the longest lateral shoots along a parent shoot allows distinguishing acrotonic (i.e. apple (Lauri 2007)) or basitonic (i.e. olive (Bongi and Palliotti 1994)) branching. Those **qualitative descriptions** can be complemented by **quantitative analyses** that permit gaining a deeper understanding of the topological relationship between the different organs that compose the plant (Guédon et al. 2001; Durand et al. 2005). The most widely used analyses for branching patterns have been **Markovian models** (Taylor and Karlin 1998) that permit the identification of homogeneous zones (i.e. parts of the shoot where buds of consecutive metamers have the same fate) within the shoot and the estimation of their characteristics, for example, zone composition and length (Guédon et al. 2001; Durand et al. 2005). Recent studies have proposed **generalized-linear models** (GLMs) to analyse the relationship between variables related to new shoots (e.g. burst, length) with one or more predictors linked to the bearer (e.g. length of the bearer shoot, node rank) (Boudon et al. 2020). Those models are easy to estimate and can be used per se or as complementary analysis to be incorporated into more complex ones (Dambreville et al. 2013).

In this study, a detailed characterization of ‘Tonda di Giffoni’ architectural development including observation of shoot emergence positions and dynamics was performed. For this, specific observations, over two successive years, were conducted to understand how plant elements are connected to each other and how they contribute to tree architecture. Those architectural information was then used to code the first hazelnut FSPM.

In this work, a focus is made on the analysis, by successive steps, of hazelnut ‘Tonda di Giffoni’ architectural development and the quantification of bud fates depending on the developmental time and location along their parent shoot, which constitute elementary knowledge required before the implementation of a model of hazelnut (*C. avellana*) architecture.

2. MATERIAL AND METHODS

2.1 Dataset

The experiment was carried out in Deruta, Perugia (Italy) in 2020 and 2021. The experimental orchard contained 140 seven-year-old own-rooted hazelnut trees (*C. avellana* Tonda di Giffoni), planted in 2014 at 4×4 m distances. Standard horticultural practices were applied. In January 2020, 104 one-year-old shoots (26 shoots per tree on 4 plants) of hazelnut trees were selected according to 4 length categories: short (Sh) when shorter than 5 cm, medium (Me) when between 5 and 20 cm, long (Lo) when between 20 and 40 cm and very long (VLo) when longer than 40 cm. On those shoots, biometrical measurements (i.e. diameter, length and number of nodes) were performed during winter. From the base to the shoot tip, at each node, the number and fates of buds were recorded. Four types of fates were known in *C. avellana*: latent bud (i.e. when no bud was present, B), vegetative bud (V), mixed bud (M) and male flower (catkins = C). Each of them can be easily recognized, on the shoot, thanks to their particular shape (Fig. 1A)

In January 2021, the same biometrical measurements and node buds’ inventory were conducted on lateral one-year-old shoots born from vegetative and mixed buds of shoots previously selected in 2020. In the following, one-year-old shoots of 2020 will be considered **parent shoots** or **bearers**, while the shoots born from their buds in 2021 will be named **children shoots**.

2.2 Structure of the analysis

A logigram was designed to formalize developmental processes involved in the generation of the growth and branching patterns in hazelnut (Fig. 2). Each box in the diagram represents a question that needs to be addressed to permit the development of a hazelnut architectural model. Developmental processes occurred at different scales: shoot scale (represented by circled boxes), node scale (square boxes) and bud scale (rhomboid boxes). The logigram started with the assumption that the first shoot was proleptic. The first question step was to estimate the number of nodes of this shoot. In the second step, the probability, for each node, being blind had to be estimated. If the node is blind, the model considers that node as latent, and the process aborts. In case the node is not blind, the probability of carrying or not a sylleptic lateral shoot had to be computed at the node scale. According to the value of this probability, different developmental options were considered (YES and NO arrows). In the

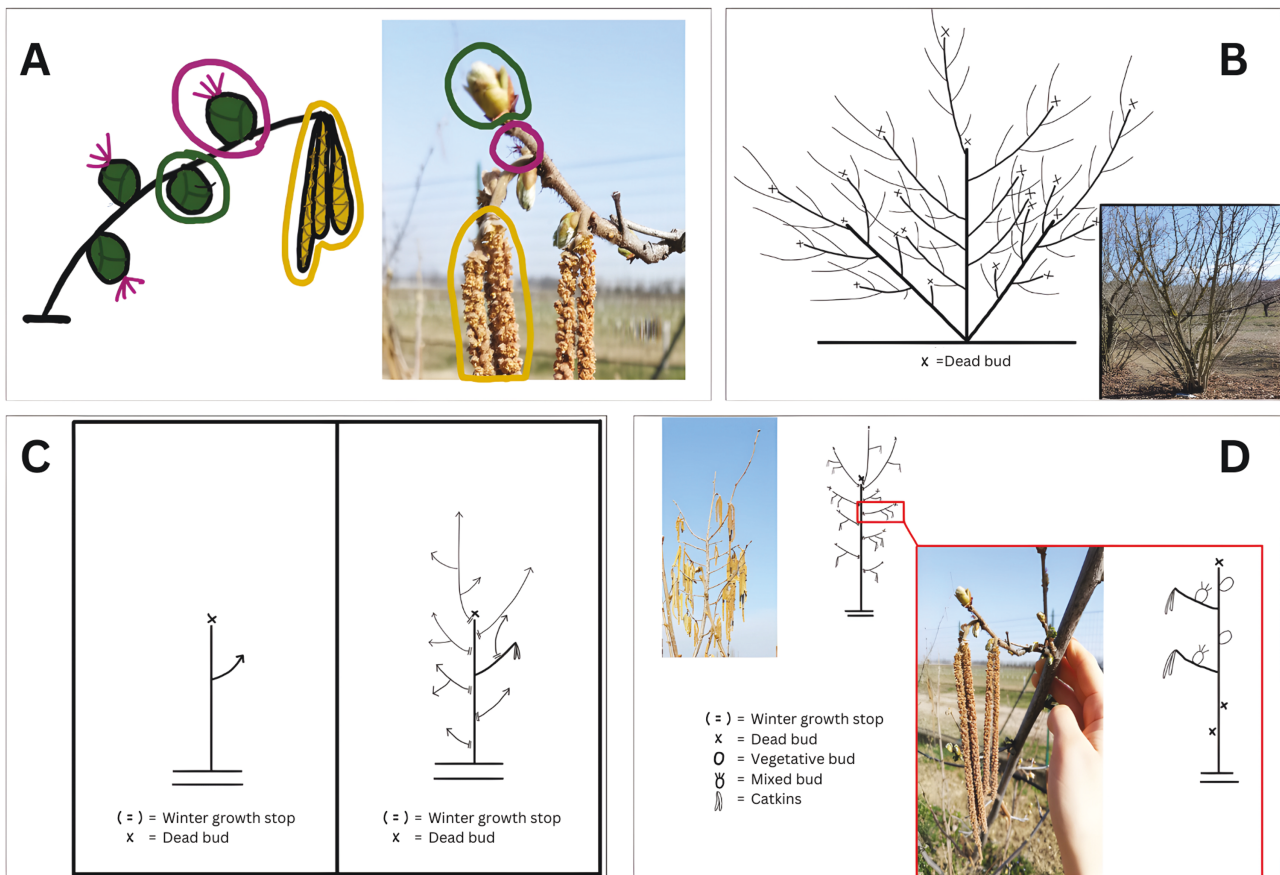


Figure 1. (A) Real picture (on the right) and simplified draw (on the left) with four types of hazelnut structures (catkins in yellow, mixed buds in pink and vegetative buds in green). (B) Schema and photo illustrating the branching behaviour in hazelnut Tonda di Giffoni, at both tree and shoot scale. (C) Schema of the development of a Hazelnut shoot Tonda di Giffoni over two successive years. (D) Schema and photos illustrating the branching pattern of a proleptic shoot and the sylleptic nature of shoots bearing catkins in hazelnut Tonda di Giffoni.

case of a sylleptic lateral shoot, the number of buds composing this shoot and, subsequently, the proportion of V and M were determined. Then the probability of bursting was considered and the length of new shoots was computed. In the opposite case (i.e. NO arrow), the number of lateral buds and their fate (i.e. V or M) were determined at each node along proleptic shoots. For the shoots developed from either mixed or vegetative buds, the length of the new lateral shoots was computed. At the very end, the logigram updated the order of the shoot considered from n (i.e. order of the bearer shoot) to $n + 1$ (i.e. order of the new shoot), to start again to the different steps for a new year of development (Fig. 2).

2.3 Statistical analyses

2.3.1 FSPM parametrization

All statistical analyses were performed using RStudio (R Core Team 2022). For each box in the logigram, exploratory analyses were performed to identify the variables that could be involved in the current phenomenon. When a bud fate was observed in the median part of proleptic one-year-old shoots, the distance of each node from the median one was considered a predictor. This distance was normalized by dividing it by the total number of nodes in the shoot. The variables selected from the exploratory analyses were, then, tested through more complex statistical

models (i.e. GLMs). The relationship between the length of a shoot in cm and the number of nodes carried by that shoot was estimated using a polynomial linear model [see Supporting Information—S1]. The probability, of a node, to be blind was computed using a binomial GLM with node rank as predictor [see Supporting Information—S2].

For estimating the probability of a node developing a sylleptic shoot, depending on the absolute value of the normalized distance from the median node rank, a binomial GLM was used (MOD1, see Supporting Information—S3). The number of buds, either in proleptic or in sylleptic shoots was estimated using a Poisson GLM [see Supporting Information—S4 and S5]. In sylleptic shoots, the number of V was estimated as the proportion of V buds, computed with a binomial GLM [see Supporting Information—S6] multiplied by the number of buds in sylleptic shoots [see Supporting Information—S7]. Then the number of M was computed subtracting the number of V buds from the total number of buds of that shoot. This strategy was chosen because there was no significant correlation between the number of V or M and any variable. In proleptic shoots, the proportion of M and V buds was estimated using a multinomial regression model (MRM) (MOD2, see Supporting Information—S7). This model was chosen because those proportions can be considered as an ordinal multinomial distribution. The probability of a bud

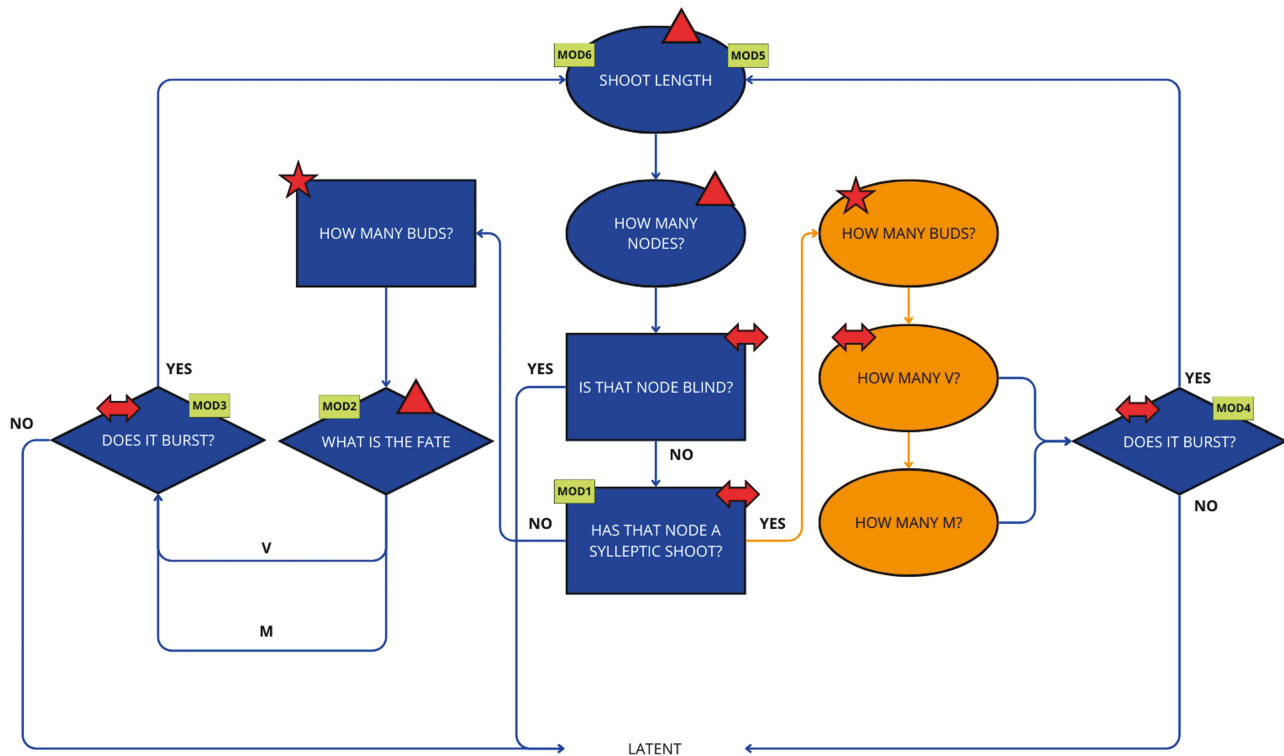


Figure 2. Logical diagram built to formalize the developmental processes involved in the generation of growth and branching in hazelnut. Each box represents a step that needs to be followed to draw the architecture of hazelnut. Different scales are possible: shoot scale (circled boxes), node scale (squared boxes) and bud scale (rhomboid boxes). Different shoots are considered: proleptic shoots (in blue) and sylleptic shoots (in orange). The red shapes represent different distributions: binomial (two arrows); Poisson (star); Gaussian, multinomial or gamma (triangle).

to burst (or not) into a new shoot was predicted using a binomial GLM with interactions with other buds in proleptic and sylleptic shoots (MOD3, MOD4, see [Supporting Information—S8 and S9](#)). The interactions were examined between the probability of bursting and the fate of the bud itself (i.e. mixed or vegetative) and the presence, in the same sylleptic shoot or in the same node, of other buds (mixed and/or vegetative). The next step was to predict the length of the new shoot. In the case of new shoots born from sylleptic shoots, ‘fitdistrplus’ package ([Delignette-Muller and Dutang 2015](#)) was used to find the best length distribution (probability density function) (MOD5, see [Supporting Information—S10](#)). The length of the new shoots from proleptic shoots was modelled using a Gaussian GLM with, as predictors, bud fate (either V or M), shoot length (cm) and normalized distance (MOD6, see [Supporting Information—S11](#)).

All the GLMs were estimated using ‘stats’ package ([R Core Team 2022](#)), while ‘nnet’ package ([Ripley and Venables 2002](#)) was used to run MRM.

Each model was first run including in the equation all the possible predictors selected through exploratory analyses. The least significant component of the equation (i.e. the one with the highest P -value) was selected and tested into a permutational model (with P -value set as 0.001) that could either exclude or maintain it in the equation, based on AIC ([Burnham and Anderson 1998](#)). AIC was used to compare several, possibly non-nested, regression models: the model with the lowest AIC was selected. However, AIC was subjected to some random noise present in data, so that AIC differences were also noisy.

The logic of permutation models consisted in removing the effect to be tested by shuffling the data set and comparing the AIC in the true data set (potentially containing the effect) with the AIC in the model obtained from the shuffled data set (not containing the effect) by construction and referred to as ‘shuffled model’. This was expected to prevent AIC differences from being explained by chance. The shuffled model had the same equation as the original model and the same dataset, except for the selected predictor, whose data were shuffled. The shuffled model was run 10 000 times and, each time the difference between its AIC and the AIC of the null model was computed. If the AIC differences between the shuffled model and the null one were lower than the AIC differences between the original model and the null model, at least in one of the permutations, the selected parameter was discarded. Then, a new model was run again excluding, from the original equation, the selected predictor. This process was reiterated until all the predictors in the equation showed significance. [Table 1](#) summarizes all the variables (either discarded, selected and not tested) for each model shown in the paper.

2.3.2 FSPM implementation

The statistical outputs of the former models (i.e. estimates, standard errors) were used to develop the first model of hazelnut architectural development. The implementation was done using L-Py ([Boudon et al. 2012](#)) in the OpenAlea platform ([Pradal et al. 2008](#)). L-Py provides a programming environment that combines L-system formalisms ([Prusinkiewicz and Lindenmayer 1990](#)) in Python language and has been already used in other

Table 1. List and description of all models estimated. For each one, the name, all the tested predictors and the final equation are mentioned. Predictors marked as X were not considered in the GLMs or MRM. Variables with NO are the ones excluded through the permutation steps (see ‘Material and Methods’ section)

Model ID	Model type	d	$ d $	D	$ D $	L	R	F	N	S	M	V	Equation of linear predictor in Y
MOD1	Binomial GLM	NO	NO	NO	YES	X	X	X	X	X	X	X	$b_0 + b_1 D $
MOD2	Multinomial regression (categories: M and V)	NO	X	X	NO	NO	YES	X	NO	X	X	X	M: $b_0 + b_1R + b_2R^{0.5} + b_3R^2 + b_4R^3 + b_5R^4$
MOD3	Binomial GLM	X	X	YES	X	NO	NO	YES	X	YES	X	X	$b_0 + b_1F_V S + b_2F_M S + b_3F_V D + b_4F_M D$
MOD4	Binomial GLM	X	NO	X	NO	NO	NO	YES	X	X	YES	YES	$b_0 + b_1F_V M + b_2F_M M + b_3F_V V + b_4F_M V$
MOD6	Gaussian GLM	X	NO	YES	NO	YES	NO	YES	X	NO	X	X	$b_0 + b_1F_V L + b_2F_M L + b_3F_V D + b_4F_M D$

d , distance from median rank node; $|d|$, absolute value of d ; D , normalized distance from median rank node; $|D|$, absolute value of D ; L , shoot length (cm)/bearer shoot length (in case of sylleptic); R , rank of node/bearer rank of node (in case of sylleptic); F , fate is k (either V or M); N , shoot length (node)/bearer shoot length (in case of sylleptic); S , other V and M buds in the same node; M , number of M buds; V , number of V buds.

fruit tree crop models (Costes *et al.* 2008; Boudon *et al.* 2020). The simulation starts in 2018 with an axiom composed of a trunk with 10 proleptic buds. Then, the juvenile phase is simulated for one year. During juvenility, the plant is mainly focussed on vegetative production (Borchert 1976). Thus, in the model, during this phase, all the buds are proleptic and vegetative. Due to the lack of data regarding the length of new shoots during the juvenility phase, this equation, in hazelnut FSPM, was obtained by changing MOD6 estimates [see Supporting Information—S11]. In particular, it increased the effect of the normalized distance from the median node rank. After the juvenile phase, in 2020, the production starts and lasts for two years as described in the previous paragraph.

2.3.3 FSPM evaluation

Model validation was performed using Python and RStudio (R Core Team 2022) by comparing the number and proportions of axillary productions, that is, blind nodes, sylleptic shoots and types of buds, between a subset of one-year-old simulated proleptic shoots and the observed datasets collected in Deruta in 2020. To perform this evaluation 1000 simulations were run in L-Py. To make the two datasets (i.e. observed and simulated) comparable, for each L-Py simulation, 104 one-year-old shoots were randomly sampled according to the same length category distribution of the observed dataset (i.e. 26 Sh shoots, 25 Me shoots, 28 Lo shoots, 25 VLo shoots). Just 576 simulations out of 1000 had enough one-year-old shoots to enable the random sampling. The number of nodes, the proportion of blind nodes, the proportion of sylleptic shoots and the proportion of M and V buds in proleptic shoots were compared between the two subsets of shoots. Prop.test of the ‘stats’ package in R (R Core Team 2022) was used to evaluate if there were significant differences in the proportion of sylleptic shoot, blind nodes and M and V buds in proleptic shoots.

3. RESULTS

The branching behaviour was observed at both the tree and shoot scales. At the tree scale, long shoots are present at the base and are responsible for its bushy global shape (Fig. 3). On the contrary, at the shoot scale, the longest lateral shoots were present in the distal position of one-year-old shoots and this was characteristic of an acrotonic gradient. The direct observation of

proleptic shoots also revealed that the apical bud died during the growing season (Fig. 1C). This suggested Tonda di Giffoni has a sympodial branching mode.

In the following, results related to the growth and branching of one-year-old shoots will be presented through two subparagraphs: the first one for sylleptic shoots, with the analysis of the production within the same year, and the second one for proleptic shoots, with the analysis of the production within the following year.

3.1 Growth and branching of sylleptic shoots

The direct observation of the developmental time of laterals revealed that the shoots bearing catkins were sylleptic shoots (Fig. 1D). This diagnostic was based on the presence of those axillary shoots prior to the other (proleptic) ones and on the absence of visible scars at their base. Moreover, those shoots were located in the median zone of the one-year-old bearer shoot. We thus used the absolute value of normalized distance, in MOD1, to estimate the probability of having a sylleptic shoot at a particular node. The maximal probability was 0.43 in the median part of the shoot and decreased toward the shoot extremities (Fig. 3 and Supporting Information—S3). The number of buds in sylleptic shoots was estimated based on the length of the bearer shoot (cm) and the absolute value of normalized distance. The total number of buds (vegetative and mixed) increased with the length of the bearer shoot and with the proximity of the median zone from a minimum of one to a maximum of seven. The proportion of vegetative was estimated using a binomial GLM [see Supporting Information—S6]. Then, the probability of each bud (either M or V) to burst was computed using MOD4. For mixed buds, the probability of bursting decreased from 0.72 to 0.06 depending on the number of other M present within the sylleptic shoot and from 0.53 to 0.18 depending on the number of other V present within the sylleptic shoot (Fig. 4 and Supporting Information—S9). For vegetative buds, the probability of bursting was not influenced by the presence of other M within the sylleptic shoot while it decreased from 0.73 to 0.13 with the number of other V present within the sylleptic shoot (Fig. 4 and Supporting Information—S9). The length of new shoots was not related to any of the tested predictors. Thus, the new shoot length distribution, born either from M or V buds, was approximated to a Gamma distribution with $\alpha = 2.37$ and $\beta = 1.20$ (Fig. 5, Supporting Information—S10).

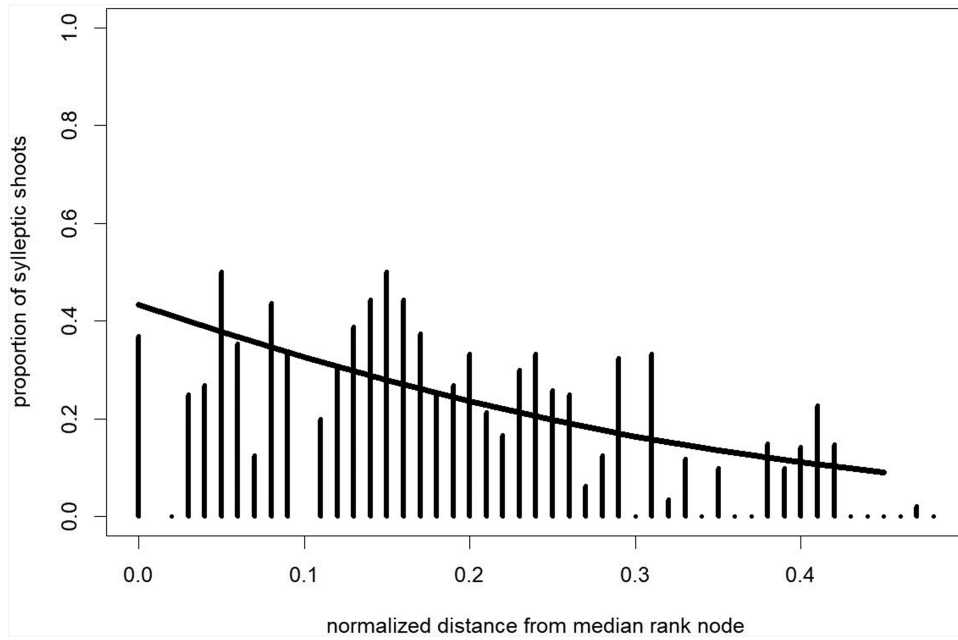


Figure 3. MOD1. Proportion of sylleptic shoots developed per node rank (computed as number of sylleptic shoots/total number of nodes), along a one-year old shoot of hazelnut Tonda di Giffoni, depending on the absolute value of the normalized distance of the current node from the median node of the parent shoot (computed as distance from median rank node/total number of nodes of the parent shoot). Bars represent observed data while the line corresponds to the MOD1 GLM equation.

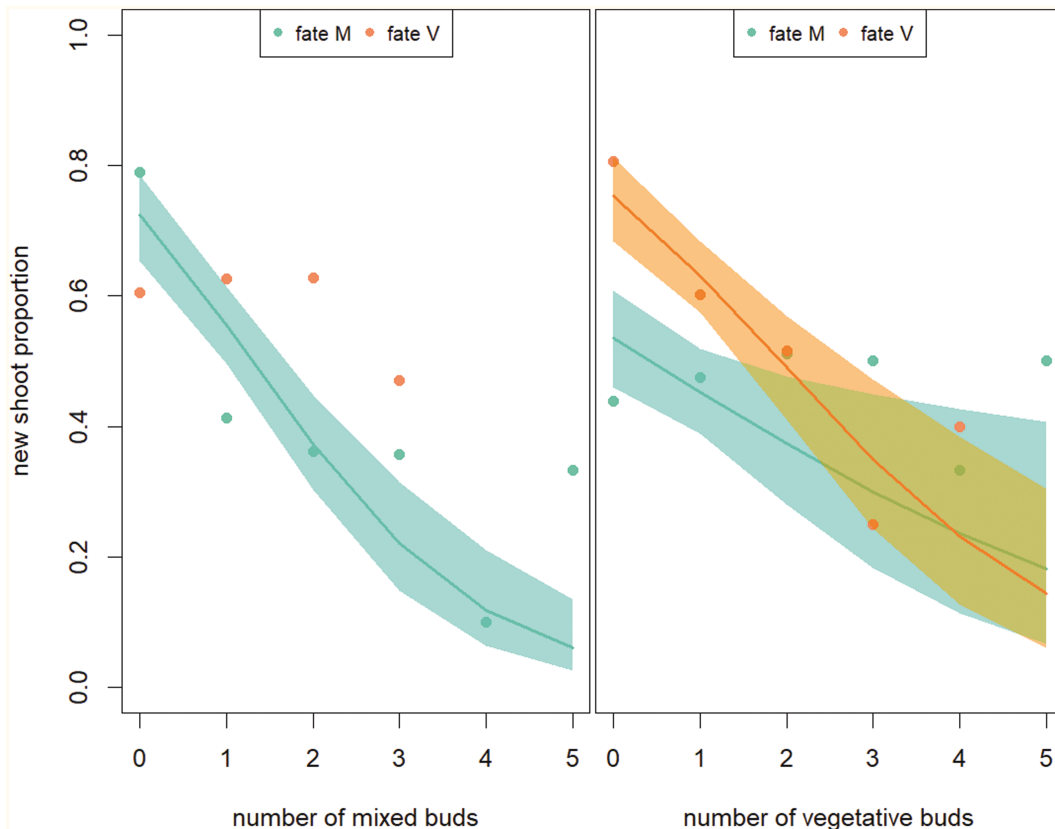


Figure 4. MOD4. Proportion of new shoots developed from sylleptic shoots of hazelnut Tonda di Giffoni, depending on the bud fate (V or M) and the presence of other M or V buds in the same sylleptic. GLMs output shows significance in the interaction between fate M and the presence of other buds (either M or V) and in the interaction between fate V and other M buds. Points represent the observed data while lines represent the predicted values with confidence interval, using MOD4 GLM equation.

3.2 Growth and branching of proleptic shoots

The nodes that did not bear a sylleptic shoot had one or more axillary buds at each node. The mean number of buds (i.e. M , V) per node rank was equal to 1.13 ± 0.02 (\pm standard error). Then, the proportion of each bud type at a given node was estimated by MOD2, that is, a multinomial regression (Fig. 6 and

Supporting Information—S7). Mixed buds (M) were mostly located (0.68%) at the median part of the shoot (rank 4–11) and less frequent (0.34%) in the proximal and distal parts (ranks < 4 and > 11 , respectively). Vegetative buds had their maximum frequency (0.60%, 0.54%) in the proximal and distal parts of the shoot (rank < 4 and rank > 13 , respectively) (Fig. 6 and Supporting Information—S7).

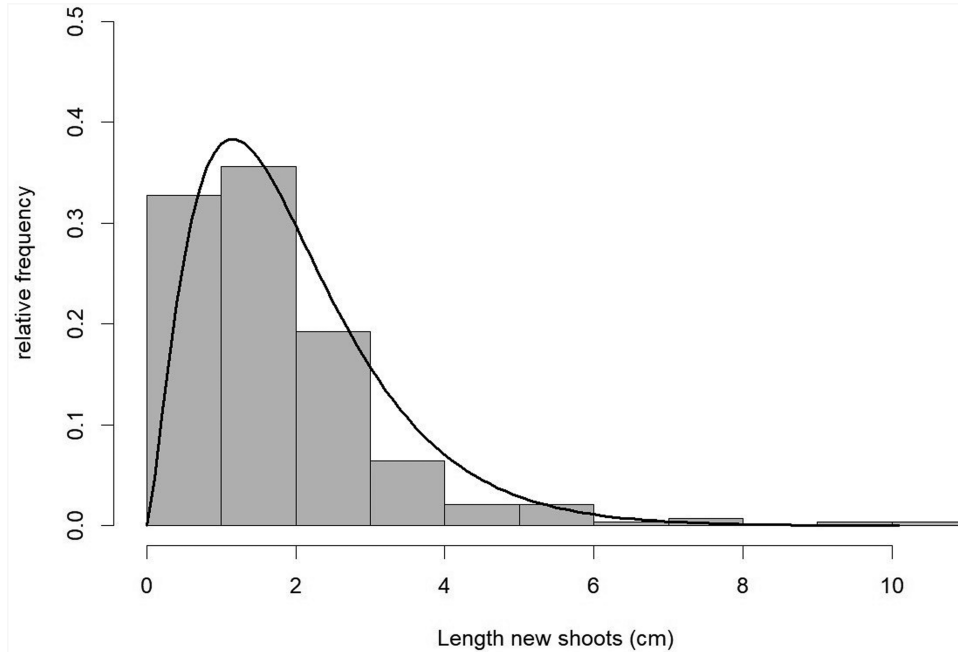


Figure 5. MOD5. Density distribution of length of new shoots, born in sylleptic shoots of Hazelnut Tonda di Giffoni, whatever the type of bud (M or V). The distribution of length follows a gamma distribution with $\alpha = 2.38$ and $\beta = 1.20$.

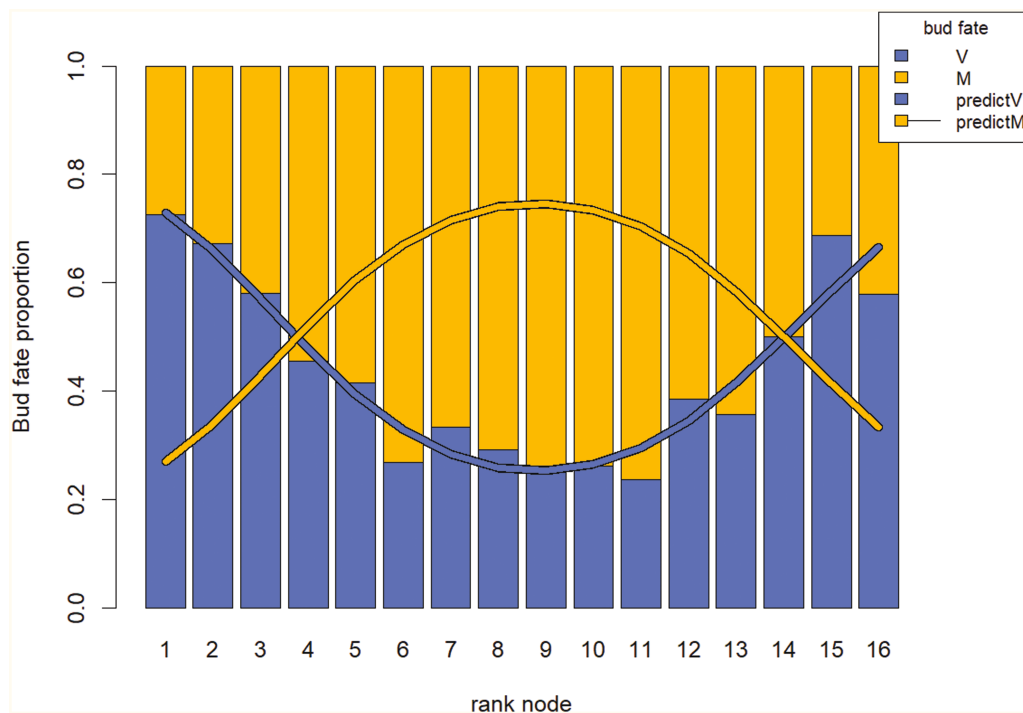


Figure 6. MOD2. Proportion of bud types (V , M) present at a node along a one-year old proleptic shoot of hazelnut Tonda di Giffoni, depending on the parent rank node. Blue and yellow boxes represent the proportion of V and M respectively while the blue and yellow lines represent their predicted values, respectively, using MOD2 GLM equation.

Regarding the probability of bud burst, if the fate of the axillary bud was blind (B), there was no shoot to be developed and the probability was zero. If the fate was either V or M, the probability of bursting was computed by MOD3. The probability of V buds bursting depends on their position on the shoot. It decreased from 0.97 to 0.62 from the distal to the proximal part, independently from the presence of other buds at the same node. However, the presence of other buds (either M or V) in the same node decreased the bursting probability. For example, in the distal part, the probability decreased from 0.97 to 0.02 when the number of other buds in the same node (either M or V) increased from zero to eight (Fig. 7, Supporting Information—S8). The probability of M buds bursting depends on their position on the shoot. It decreased from 0.96 to 0.68 from the distal to the proximal part, independently from the presence of other buds at the same node. However, the presence of other buds (either M or V) in the same node decreased the bursting probability. For example, in the distal part, the probability decreased from 0.96 to 0.03 when the number of other buds in the same node (either M or V) increased from zero to eight (Fig. 7, Supporting Information—S8).

When all the proleptic buds, whether they will sprout or not, were considered, the mean number of lateral shoots per node increased with node rank from 0.78 ± 0.05 (\pm standard error) to 1.30 ± 0.15 (\pm standard error) whatever they were bearing more than one bud or not [see Supporting Information—S12]. When nodes with at least one lateral shoot were considered only, the mean number of lateral shoots per node was no longer affected by the node rank and was 1.03 ± 0.01 (\pm standard error) [Supporting Information]. However, in both cases, the

mean number of laterals per node presented a large variation depending on the total number of buds (either V or M) at the node. Indeed, this mean number of laterals increased with the number of buds per node, and when all buds were considered, it varied from 0.89 ± 0.04 (\pm standard error) to 4.65 ± 1.75 (\pm standard error) from nodes with one bud to nodes with nine buds [Supporting Information—S12]. This mean number slightly varied when we considered nodes with one lateral at least (from 1.01 ± 0.04 (\pm standard error) to 4.14 ± 1.58 (\pm standard error)) from nodes with one to nine buds [see Supporting Information—S13].

The length in cm of the new lateral shoots (Fig. 8) was estimated by MOD6. It varied depending on the type of the bud from which the shoot was born (V or M), on the length of the bearer shoot, and the normalized distance from the median node rank. The length of new shoots developed from V buds was 4.14 ± 0.29 cm (\pm standard error) on average but largely depended on the node rank. It decreased from 6.84 ± 0.28 cm when the bud was located in distal position to 0.58 ± 0.35 cm in proximal position (Fig. 8 and Supporting Information—S11). The length of new shoots developed from V buds also depended on the bearer shoot length. It increased from 2.13 ± 0.25 cm when the bearer shoot was short (5 cm) to 6.52 ± 0.33 cm for long bearer shoots (70 cm) (Fig. 8 and Supporting Information—S11). The length of new shoots developed from M buds was 2.89 ± 0.08 cm on average and was shorter than those developed from V buds. As for laterals developed from V buds, it depended on the node rank and the bearer shoot length. It decreased from 3.42 ± 0.30 cm to 1.96 ± 0.40 cm when the bud was located in a distal or proximal position, respectively

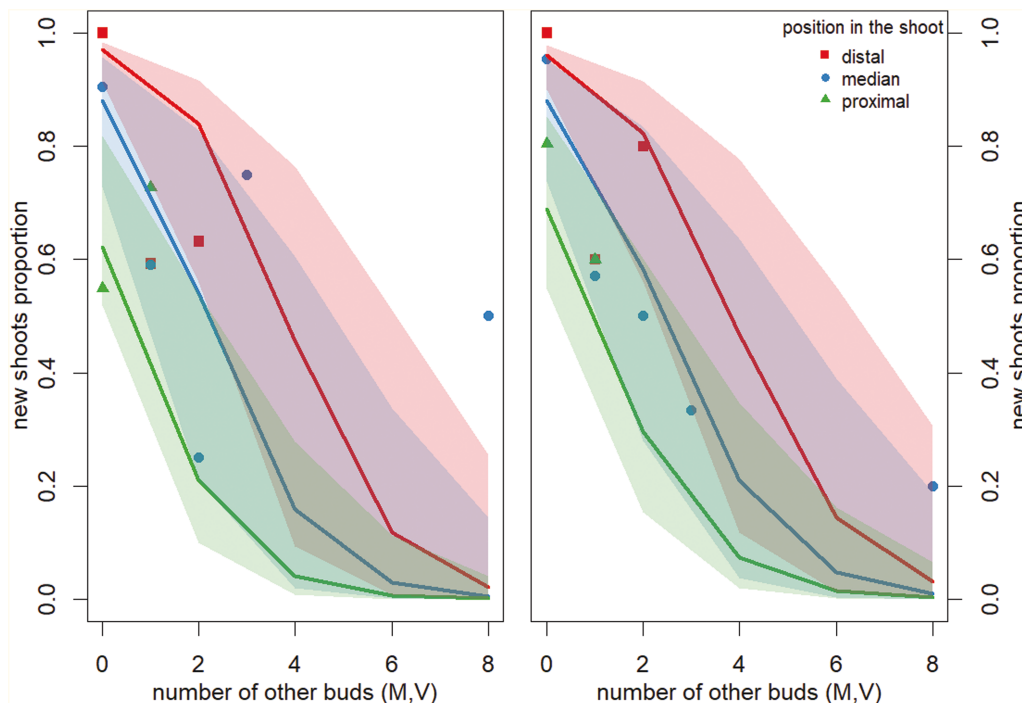


Figure 7. MOD3. Proportion of new shoots developed at a node along a one-year old shoot of hazelnut Tonda di Giffoni, depending on the presence of other buds at the same node (either M or V), and the normalized distance of the node from the median node of the parent shoot. On the left: proportion of new shoots from V buds; on the right: proportion of new shoots from M buds. Different colours represent different normalized distances: red = distal position, blue = median position, green = proximal. Squares, dots and triangles represent observed data while lines represent the predicted values with their confidence interval, using MOD3 GLM equation.

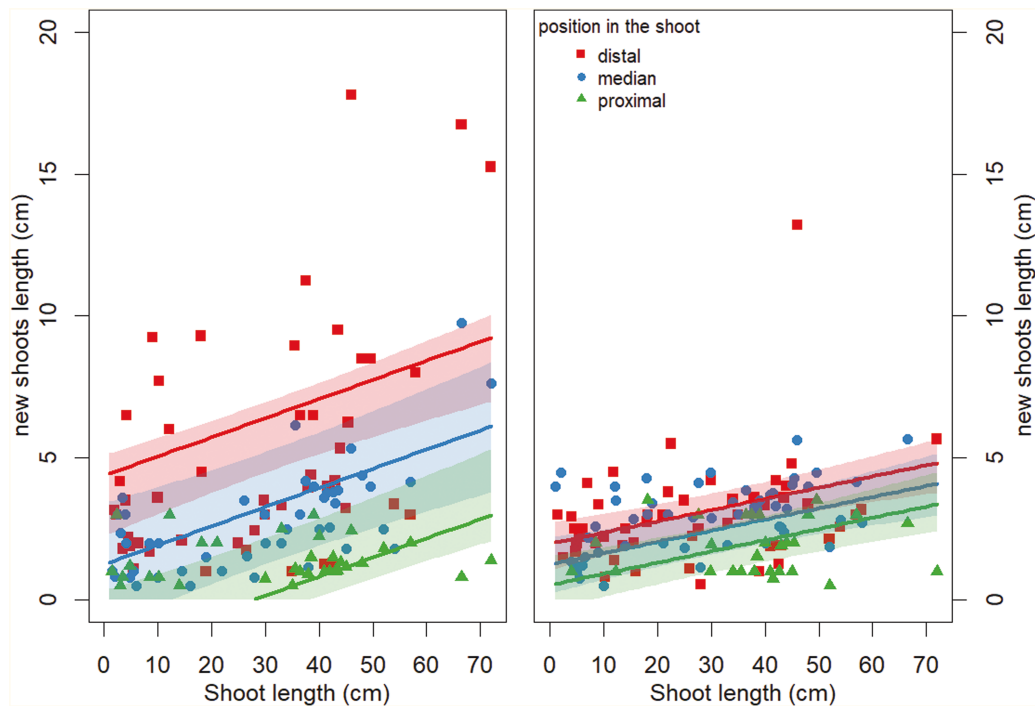


Figure 8. MOD6. Length of new lateral shoots developed at a node along one year old proleptic shoots of hazelnut Tonda di Giffoni, depending on bud fate, parent shoot length and the normalized distance of the node from the median rank node of the parent shoot. On the left: length of new shoots from V buds; on the right: length of new shoots from M buds. Different colours represent different normalized distances: red = distal position, blue = median position, green = proximal. Squares, dots and triangles represent real data while lines are the predicted values and their confidence interval, using MOD6 GLM equation.

(Fig. 8 and Supporting Information—S11). The length of new shoots developed from M buds increased from 1.57 ± 0.24 (\pm standard error) to 4.15 ± 0.32 cm when the bearer shoot was short (5 cm) or long (70 cm), respectively (Fig. 8 and Supporting Information—S11).

3.3 Model evaluation

The overall correlation between the length of one-year-old shoots and the number of nodes is similar in the observed and simulated datasets. All the black points (i.e. observed data) appear to be in the range of the simulated data (i.e. red dots) (Fig. 9). However, when shoot length is between 10 cm and 25 cm, the simulated number of nodes is overestimated (P -value < 0.05 , t -test). In fact, the simulated number of nodes is 8.71 ± 0.02 while the observed number of nodes is 8.00 ± 0.31 . The proportion of blind nodes was slightly but statistically different (P -value < 0.05) between observed and simulated data (0.13 and 0.11, respectively) (Fig. 10). The proportion of sylleptic shoots was comparable and not statistically different between observed and simulated data (0.22 and 0.23, respectively) (Fig. 11). The proportion of mixed and vegetative buds, along one-year-old proleptic shoots, was in a similar range between observed and simulated data: 0.46 and 0.48, for mixed buds (Fig. 10C); 0.40 and 0.41, for vegetative buds (Fig. 10C).

4. DISCUSSION

Few attempts have been made so far to investigate the activity of meristems in hazelnut trees to understand the tree and shoot

development. Although it was already described that catkins were located laterally on proleptic shoots (Germain and Sarraquigne 2004), we clarified that they are located terminally only on shoots that had grown in the same year as the parent shoot and therefore are sylleptic shoots (Fig. 1D). Indeed, throughout direct observations and measurements, we noticed that catkins are present in the apical position of quite short shoots, with five to six axillary buds. Furthermore, the branching of hazelnuts has been previously described, at the tree level, as basitonic (Botta and Valentini 2018). Here, we proposed to make a distinction between the branching mode at tree scale and at shoot scale (Fig. 1B and C) as suggested by Germain and Sarraquigne (2004). Our observation clearly highlighted that a basitonic branching at the tree scale is compatible with an acrotonic at the shoot scale. While acrotony is usually considered as being driven by apical dominance, the basitony and the activation of buds at the tree base have generated few investigations. Even though Champagnat (1978) has described basitony as an autumnal gradient, resulting from a higher axillary bud growth potential of basal buds prior to dormancy, which is inverted during winter in acrotonic species contrary to basitonic species (Champagnat 1978), the physiological conditions in which such a gradient is established and maintained after dormancy are still to be investigated. In addition, few studies have been carried out for defining if hazelnut branching mode was monopodial (i.e. when the apical meristem remains alive and dominant) or sympodial (i.e. when the apical meristem dies) (for a review, see Costes *et al.* (2006)). Solar and Štampar (2005) have observed a sympodial branching on two Slovenian cultivars, 'Istrska dolgoplodna leska' and

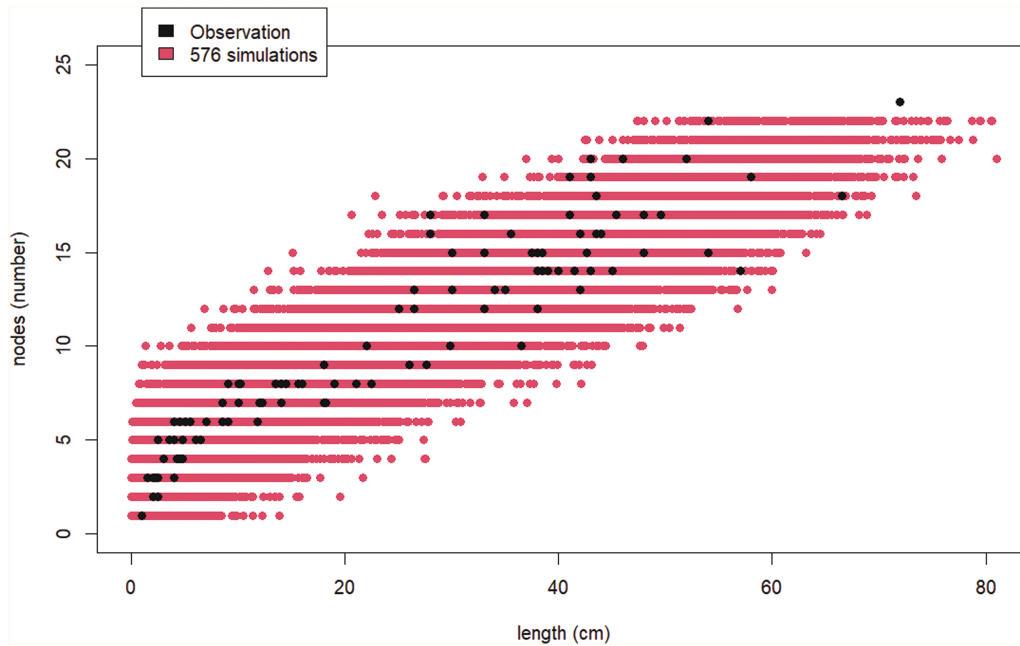


Figure 9. Number of nodes of one year old proleptic shoots of hazelnut Tonda di Giffoni, depending on their length. Different colours represent different datasets: black = data observed in Deruta fields in January 2020; red = data obtained from 576 simulations in L-Py using [Supporting Information—S1](#) linear equation.

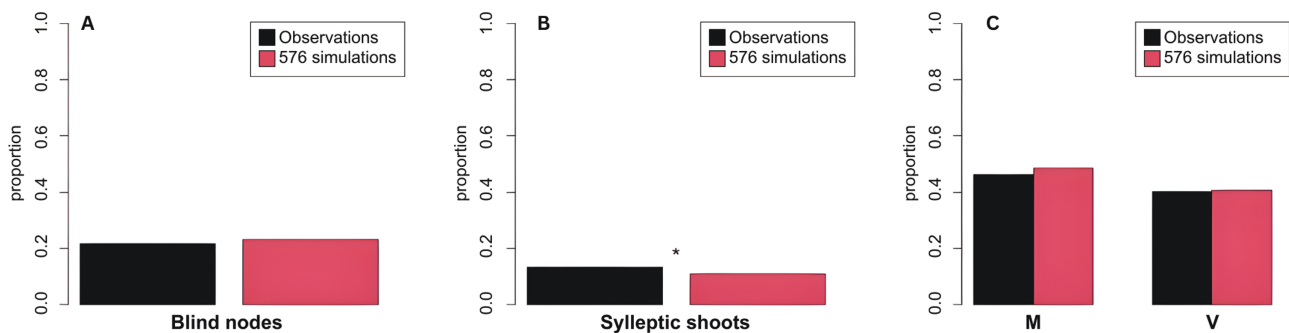


Figure 10. (A) Proportion of blind nodes in one year old proleptic shoots of Hazelnut Tonda di Giffoni. Different colours represent different datasets: black = data observed in Deruta fields in January 2020; red = data obtained from 576 simulations in L-Py using [Supporting Information—S2](#) linear equation. (B) Proportion of nodes with sylleptic shoots in one year old proleptic shoots of Hazelnut Tonda di Giffoni. (C) Proportion of M and V buds in one year old proleptic shoots of Hazelnut Tonda di Giffoni.

‘Pauetet’. In the current study, we consistently observed a sympodial branching mode in *C. avellana* Tonda di Giffoni where the death of the apical bud was observable in proleptic shoots during the growing season ([Fig. 1C](#)).

We used a logigram to organize the successive steps that need to be considered for modelling shoot growth and branching depending on the shoot and bud types ([Fig. 2](#)). This approach, previously used to implement the FSPM V-Mango, was helpful in the hazelnut case as the elementary processes are shared among species. In hazelnuts, the branching pattern was found to be organized by zones along the bearer shoot, as previously found in several fruit species (apple tree ([Guédon et al. 2001](#)), peach tree ([Fournier 1994](#)), almond ([Negrón et al. 2013](#)) and apricot ([Costes and Guédon 1996](#))). Sylleptic shoots were found more frequently in the middle part of the shoot. This is in accordance with previous literature on the above-mentioned fruit species, but also on the hazelnut where in another cultivar, ‘Tonda

Gentile delle Langhe’, the male flowers have been described as being mainly in the median part of the shoots ([Tombesi and Farinelli 2014](#)). On the proleptic shoots, mixed buds (M) were also present mainly in the median part of the shoot. Such a location has been previously described along a neoformed parts in several prunus trees, such as peach and almond ([Costes et al. 2014](#)). However, this result appears contradictory with previous literature on another cultivar of hazelnut, ‘Tonda Gentile delle Langhe’, where female flowers have been found mainly in the distal part of the shoot ([Tombesi and Farinelli 2014](#)). This suggests that the difference among hazelnut cultivars should be further investigated. The hazelnut branching pattern also included the presence of the longest new shoots in the distal part of the parent shoot. This was consistent with the visual observation of the tree shape ([Fig. 1B](#)). This acrotonic behaviour at the shoot level is in accordance with what is described in literature ([Tombesi 1985](#); [Germain and Sarraquigne 2004](#)).

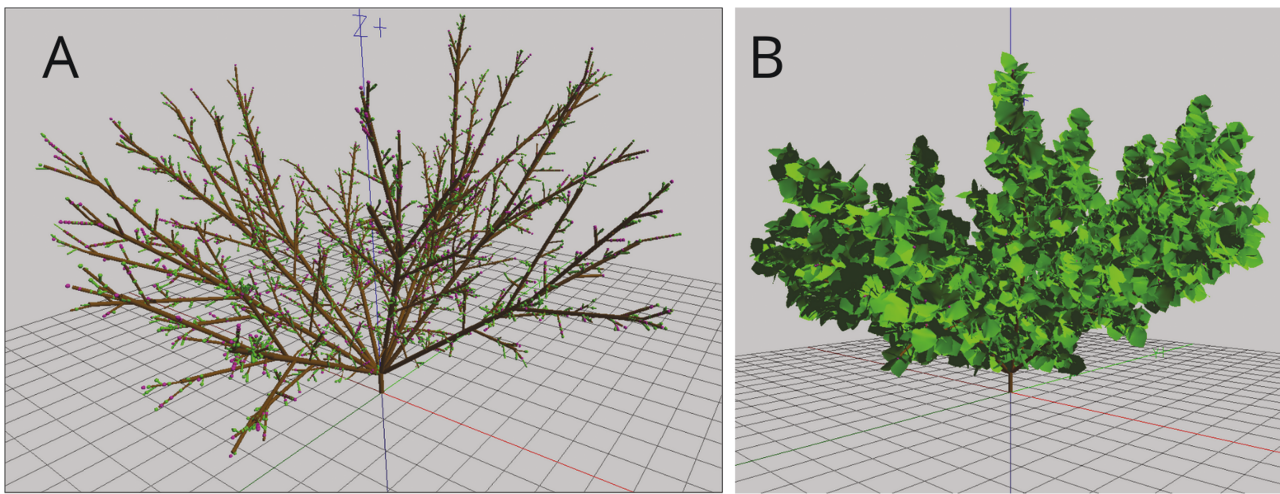


Figure 11. Visual result of Tonda di Giffoni FSPM. The architecture is simulated over two successive years in L-Py. The simulation was run without leaves (A) and with leaves (B).

The new shoot lengths were found to depend on the type of buds they were coming from, with longer shoots developing from V buds than those developing from M buds. This may result from the determinate and preformed nature of the mixed shoots developing from M buds, with the female flower located in the terminal position (Germain and Sarraquigne 2004). On the contrary, the shoots developing from V buds are constituted of a preformed part but are likely to include neoformed part, even though the number of preformed organs remains to be determined (Gordon *et al.* 2006). We have sampled one-year-old shoots at the tree periphery, on seven years old trees. Therefore, additional observations and measurements on the basal and central part of the trees would be required to complement the current dataset and analyses with longer bearer and children shoots.

In nature, there are many species that have more buds at the same node (Bell and Bryan 1991). In *Prunus* spp. one vegetative structure (i.e. vegetative bud or sylleptic shoot) could be associated with one or more reproductive structures (i.e. female flowers) (Costes *et al.* 2014). In *Vitis vinifera*, the same node can bear a prompt mixed bud and a compound latent bud (Vasconcelos *et al.* 2009). The current study assessed that in hazelnut, several vegetative buds, or mixed buds or a combination of the two could be present at a given node. Most usually, when there are multiple buds per node, one of them is more outstanding than the others and it will be the only one to burst, as described in *Eucalyptus* spp. (Bell and Bryan 1991) and at the compound bud axil of *V. vinifera* (Vasconcelos *et al.* 2009). This could result from competition between buds, for resources such as carbohydrates and water (Rameau *et al.* 2015) as it was suggested for *Juglans regia* (Bonhomme *et al.* 2010) and *Prunus armeniaca* (Costes and Guédon 1996). However, there are cases in which two buds or more, present at the same node, could develop into different structures. In *Leucaena* spp. all axillary floral buds develop into inflorescences (Bell and Bryan 1991). In hazelnut, when there is more than one bud at the same node, most frequently just one of them will develop into a shoot (Fig. 7). However, when just vegetative buds are present (i.e. no mixed buds associated), two or more of them could burst in the successive year (data not shown for proleptic shoots). This phenomenon could result from a

greater competition between reproductive (flowering and fruiting) and vegetative growth than between two growth units as it has been suggested for *P. armeniaca* (Costes and Guédon 1996).

4.1 Model evaluation

The relationship between the length of one-year-old shoots and the number of nodes could be simulated with an acceptable accuracy when comparing the overall correlation between these two variables in observed and simulated data. Despite the simulated data included observations, when the shoot length was between 10 cm and 25 cm, the simulation had an overestimated number of nodes (8.71 ± 0.02 and 8.00 ± 0.31 , simulated and observed data, respectively) (Fig. 9). This problem could be due to two reasons: the first is the reduced sample size (i.e. 104 one-year-old shoots, approximately 25 shoots per length category). A larger sample size could lead to a more precise estimation of the correlation between length and number of nodes. Secondly, the lack of information of the architectural rules during the juvenile phases of the hazelnut tree has forced us to obtain such rules changing MOD6 equation (Supporting Information—S11). This inference could not be correct because tree architectural traits and rules could change as the plant grows (de Reffye *et al.* 1988; Barthélémy *et al.* 1989). In addition, the model underestimates the proportion of blind nodes on proleptic shoot (Fig. 10) while the proportion of sylleptic shoot and mixed and vegetative buds is correctly simulated (Figs. 10B and 10C). Again, enhancing the sample size and repeating the same experiment for a larger number of years could reduce the model errors and improve the evaluation process.

6. CONCLUSIONS AND PERSPECTIVES

A first developmental FSPM of hazelnut growth and branching was built (Fig. 11). The development of hazelnut buds and shoots was monitored over two successive years. The logical diagram proposed, and the equations presented in this study were used to draw the visual representation of hazelnut development, in L-Py through L-systems formalism (Prusinkiewicz and Lindenmayer 1990). However, the evaluation analysis suggested

that such a structural model will need additional field experiments to collect and estimate the architectural behaviour of the tree during the juvenile phase (Borchert 1976) and over a larger number of years. For this, observations should be collected over multiple successive years or on trees of different ages, to have a better view of how architectural traits change over time. Further studies will also be required to create a functional model that describes carbon partitioning within the tree in order to merge the architectural model with the functional one to obtain a more complex FSPM of hazelnut.

SUPPORTING INFORMATION

The following additional information is available in the online version of this article –

Figure S1. Estimates of model of the relationship between shoot length (cm) and number of nodes. Parameters ($b_1 = \text{length}^{0.5}$, $b_2 = \text{length}^2$) used to predict the number of nodes of a shoot from its length. Predictors are the length in cm at the power of 0.5 and 2. See Statistics section in Material and Methods for model selection method. Equation Y: $b_1 * L^{0.5} + b_2 * L^2$.

Figure S2. Estimates of model to compute the probability of having a blind node. Parameter ($b_1 = \text{rank node}$) used to predict the probability of that node of being blind. Predictor is the rank of the concerned node. See Statistics section in Material and Methods for model selection method. Family is “binomial”. Equation of linear predictor in Y: $b_1 * R$.

Figure S3. Estimates of MOD1 parameters ($b_1 = |\text{normalized distance from median rank node}|$) used to predict the proportion of sylleptic shoots that develop from a proleptic shoot node. Predictor is the absolute value of the normalized distance of the current node from the median rank node of the parent shoot. See Statistics section in Material and Methods for model selection method. Family is “binomial”. Equation of linear predictor in Y: $b_1 |D|$.

Figure S4. Estimates of model to compute number of buds in sylleptic shoot. Parameter ($b_0 = \text{intercept}$, $b_1 = \text{bearer length (cm)}$, $b_2 = |\text{normalized distance from median rank node}|$) used to predict the number of buds in sylleptic shoot. See Statistics section in Material and Methods for model selection method. Family is “poisson”. Equation of linear predictor in Y: $b_0 + b_1 * L + b_2 * |D|$.

Figure S5. Estimates of model to compute number of buds in proleptic shoot. Parameter ($b_0 = \text{intercept}$) used to predict the number of buds in proleptic shoot. See Statistics section in Material and Methods for model selection method. Family is “poisson”. Equation of linear predictor in Y: b_0 .

Figure S6. Estimates of model to compute the proportion of vegetative buds in sylleptic shoot. Parameter ($b_0 = \text{intercept}$) used to predict the number of vegetative buds in sylleptic shoot. See Statistics section in Material and Methods for model selection method. Family is “binomial”. Equation of linear predictor in Y: b_0 .

Figure S7. Estimates of MOD2 parameters (b_0 to b_5) used to predict the proportion of different buds in proleptic shoots. Parameter ($b_0 = \text{intercept}$, $b_1 = \text{rank node}$, $b_2 = \text{rank node}^{0.5}$, $b_3 = \text{rank node}^2$, $b_4 = \text{rank node}^3$, $b_5 = \text{rank node}^4$) used to predict the number of vegetative buds in sylleptic shoot. See

Statistics section in Material and Methods for model selection method. Equation of linear predictors in Y (categories are M and V). M: $b_0 + b_1 R + b_2 R^{0.5} + b_3 R^2 + b_4 R^3 + b_5 R^4$.

Figure S8. Estimates of MOD3 parameters ($b_0 = \text{intercept}$, $b_1 = \text{number of other M and V buds} * \text{fate}[V]$, $b_2 = \text{number of other M and V buds} * \text{fate}[M]$, $b_3 = \text{normalized distance from median rank node} * \text{fate}[V]$, $b_4 = \text{normalized distance from median rank node} * \text{fate}[M]$) used to predict the probability of a bud to burst in proleptic shoot. See Statistics section in Material and Methods for model selection method. Family is “binomial”. Equation of linear predictor in Y: $b_0 + b_1 FVS + b_2 FMS + b_3 FVD + b_4 FMD$.

Figure S9. Estimates of MOD4 parameters ($b_0 = \text{intercept}$, $b_1 = \text{number of other M} * \text{fate}[V]$, $b_2 = \text{number of other M} * \text{fate}[M]$, $b_3 = \text{number of other V} * \text{fate}[V]$, $b_4 = \text{number of other M} * \text{fate}[M]$) used to predict the probability of a bud to burst in sylleptic shoot. See Statistics section in Material and Methods for model selection method. Family is “binomial”. Equation of linear predictor in Y: $b_0 + b_1 FVM + b_2 FMM + b_3 FVV + b_4 FMV$.

Figure S10. MOD5 distribution of the length of the new shoots bursted from buds in sylleptic shoots.

Figure S11. Estimates of MOD5 parameters (b_0 to b_4) used to predict the proportion of new shoots that develop from a bud (M or V) in proleptic shoots. Predictors were bud fates (V or M) and their interactions with the numbers of other M or V buds at the same node and with the normalized distance of the node from the median rank node of the parent shoot. See Statistics section in Material and Methods for model selection method. Family is “gaussian”. Equation of linear predictor in Y: $b_0 + b_1 FVL + b_2 FML + b_3 FVD + b_4 FMD$.

Figure S12. Estimates of parameters (b_0 to b_2) used to predict the number of new shoots from proleptic buds (either V or M) whatever they sprout or not. Predictors were rank node and number of other buds (either V or M) at the same node. Family is “poisson”. Equation of linear predictor in Y: $b_0 + b_1 R + b_2 S$.

Figure S13. Estimates of parameters (b_0 to b_1) used to predict the number of new shoots (from proleptic buds (either V or M), considering just sprouted buds. Predictors were number of other buds (either V or M) at the same node. Family is “poisson”. Equation of linear predictor in Y: $b_0 + b_1 S$.

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CONFLICT OF INTEREST STATEMENT

None declared.

DATA AVAILABILITY

Data are available in the open source GitHub repository: <https://github.com/Corilana/L-HAZELNUT>.

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